

**MATEMATYKA  
DYSKRETNA**

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Preprint Nr MD 042  
(otrzymany dnia 26 I 2009)

**Kraków  
2009**

Redaktorami serii preprintów *Matematyka Dyskretna* są:  
Wit FORYŚ,  
prowadzący seminarium *Słowa, słowa, słowa...*  
w Instytucie Informatyki UJ  
oraz  
Mariusz WOŹNIAK,  
prowadzący seminarium *Matematyka Dyskretna - Teoria Grafów*  
na Wydziale Matematyki Stosowanej AGH.

# Total weight choosability of graphs\*

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January 27, 2009

## Abstract

Suppose the edges and the vertices of a simple graph  $G$  are assigned  $k$ -element lists of real weights. By choosing a representative of each list, we specify a vertex colouring, where for each vertex its colour is defined as the sum of the weights of its incident edges and the weight of the vertex itself. How long lists ensures a choice implying a proper vertex colouring for any graph? Is there any finite bound or maybe already lists of length two are sufficient? We prove that 2-element lists are enough for trees, wheels, unicyclic and complete graphs, while the ones of length 3 are sufficient for complete bipartite graphs. Our main tool is an algebraic theorem by Alon called Combinatorial Nullstellensatz.

**Keywords:** graph labelling, neighbour distinguishing total weighting, total list weighting, vertex colouring

**MSC:** 05C78